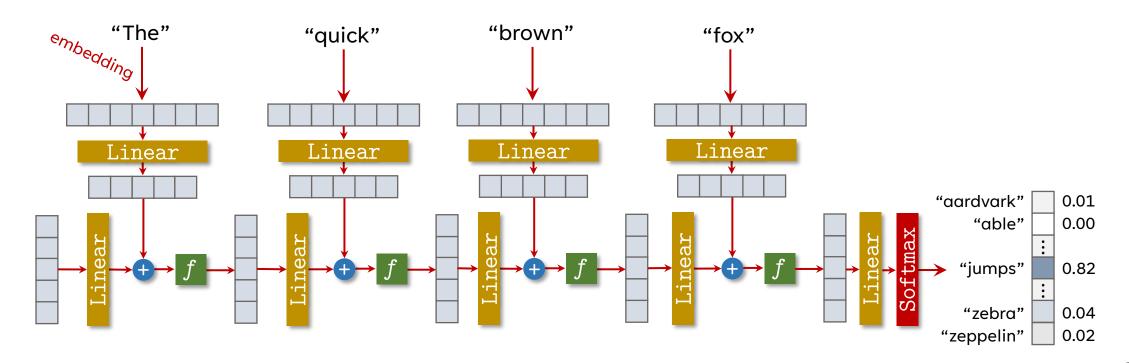


Lecture 5: LSTMs and GRUs

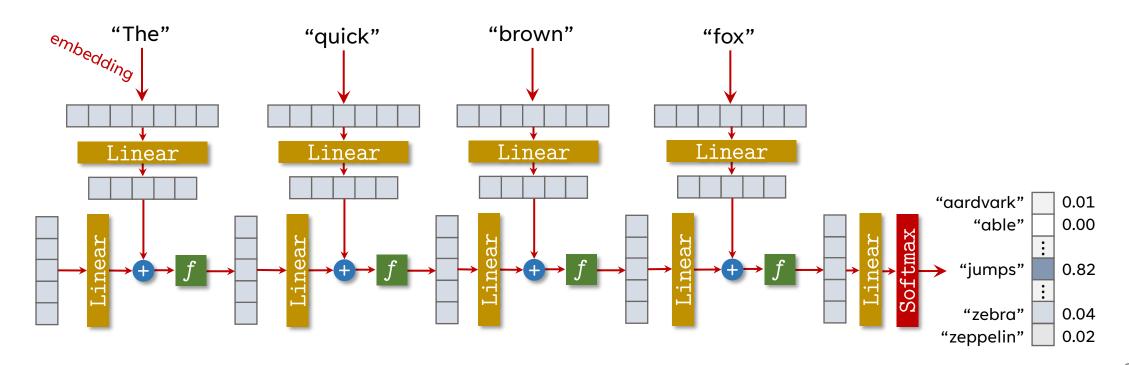
RECAP FROM PREVIOUS LECTURE

• We discussed the recursive neural network (RNN) architecture.



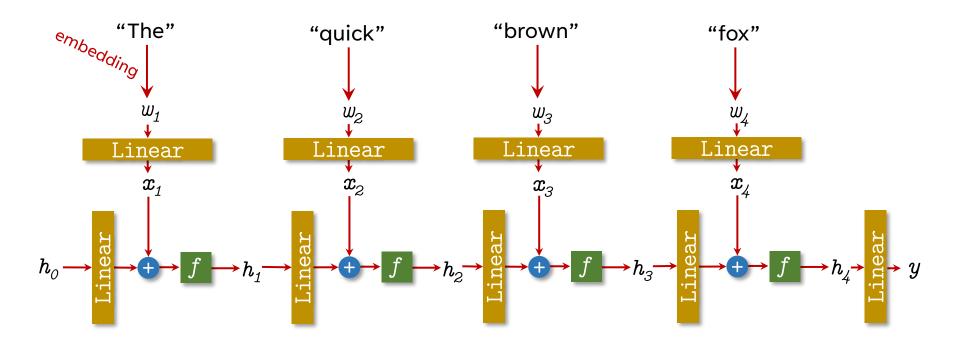
RECAP FROM PREVIOUS LECTURE

• Models the sequential (word-by-word) processing nature of human language processing.



RECAP FROM PREVIOUS LECTURE

• Models the sequential (word-by-word) processing nature of human language processing.



VANISHING/EXPLODING GRADIENTS

Suppose we have a long RNN (lots of tokens).

$$y = g_n(g_{n-1}(\ldots g_2(g_1(x_1, W_1))\ldots))$$

- Each g_i is an RNN "unit", written more simply.
- x_1 is the first word, and W_1 is the weight matrix in the linear layer after x_1 .
- What is the gradient with respect to W_1 ?

$$\nabla_{W_{1}} \mathbf{y} = g_{n}'(...) \cdot \nabla_{W_{1}} g_{n-1}(...)$$

$$= g_{n}'(...) \cdot g_{n-1}'(...) \cdot \nabla_{W_{1}} g_{n-2}(...)$$

$$= ... = g_{n}'(...) \cdot g_{n-1}'(...) \cdot ... \cdot g_{2}'(...) \cdot g_{1}'(...) \cdot \mathbf{x}_{1}^{\mathrm{T}}$$

VANISHING/EXPLODING GRADIENTS

- Note that this is a product containing many terms.
- If the terms are > 1, their product will grow exponentially in n.
- If the terms are < 1, their product will shrink to 0 exponentially in n.
- This is called the exploding or vanishing gradient problem.
- This is also an issue for very deep networks (containing many layers).

$$\nabla_{W_{1}} \mathbf{y} = g_{n}'(...) \cdot \nabla_{W_{1}} g_{n-1}(...)$$

$$= g_{n}'(...) \cdot g_{n-1}'(...) \cdot \nabla_{W_{1}} g_{n-2}(...)$$

$$= ... = g_{n}'(...) \cdot g_{n-1}'(...) \cdot ... \cdot g_{2}'(...) \cdot g_{1}'(...) \cdot \mathbf{x}_{1}^{\mathrm{T}}$$

- Suppose we have some NLP task where the input is a document or string of words.
- If the expected output for this task requires information about words that occur far from the end of the input,
 - This is a long-term dependency (or a long-range dependency).
- Why are they important in natural language?

- Consider the following sentences:
 - "The cat, which was very hungry, chased the mouse."
 - "The children sitting under the tree know the farmers."
- Suppose we ask questions such as:
 - Who chased the mouse?
 - Who knows the farmers?

- Consider the following sentences:
 - "Without her contributions would be impossible."
 - What is the subject of this sentence?
 - What is the main verb?
 - "The old man the boat."
 - "I convinced her children are noisy."
 - (I convinced her that children are noisy)
- These are called garden path sentences.

- Long-term dependencies appear in almost every NLP task.
- Coreference resolution:
 - "I couldn't fit the trophy in the bag because it was too big."
- Translation:
 - Consider translating from an SVO language into an VSO language.
 - E.g., English into Arabic.
 - "The cat, which was very hungry, chased the mouse"
 - ["chased"] ["the cat, which was very hungry"] ["the mouse"]

- It is possible for an RNN to compute long-term dependencies.
- For example, we can construct an RNN to memorize the input sequence:
 - Input: word embedding w_t and previous state h_{t-1}
 - Suppose hidden dimension is Nd
 - where N is the sequence length, and d the embedding dimension.
 - The linear layer on the word simply takes the embedding of w_t and appends many zeros to the end of it.
 - The first d elements of the output are the embedding of w_t , and the last (N-1)d elements are zero.
 - The linear layer on the hidden state rotates the dimensions of h_{t-1} by d positions.

- It is possible for an RNN to compute long-term dependencies.
- For example, we can construct an RNN to memorize the input sequence:
 - Input: word embedding w_t and previous state h_{t-1}
 - This construction is simply concatenating each word embedding into a long hidden state vector (which is initially zero).
 - Therefore, the hidden state is able to keep track of long-term dependencies.
 - It has memorized the entire input!

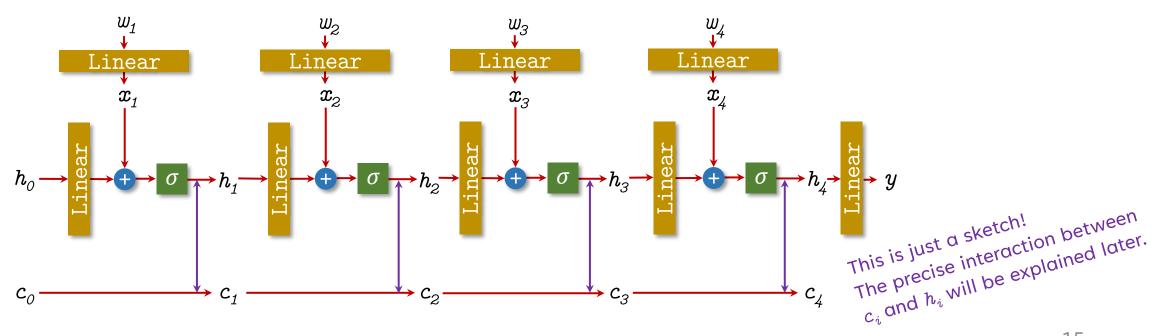
EXPRESSIVENESS VS LEARNABILITY

- It is possible for an RNN to compute long-term dependencies.
- In fact, RNNs are *Turing-complete* (Siegelmann 1995).
- A model is Turing-complete if for any Turing machine M (i.e., algorithm),
 There exists an instance of the model that implements M.
 I.e., there is a setting of the model weights such that it implements M.

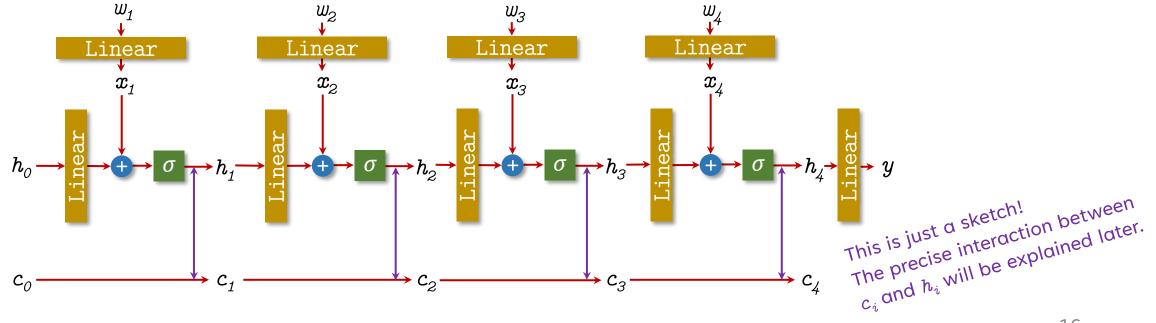
EXPRESSIVENESS VS LEARNABILITY

- The problem is that this network is difficult to learn.
 - Due to the vanishing/exploding gradients problem.
- But this is a common problem with highly expressive models.
 - E.g., MLPs, RNNs, transformers
 - These models are able to express a vast number of algorithms.
 - But the question of whether they can learn all such algorithms from data is entirely separate.
 - Oftentimes, there are algorithms that these models can express, but have difficulty learning.

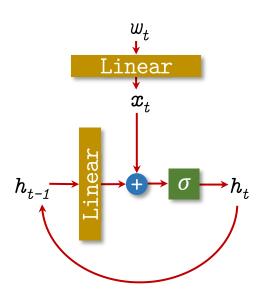
• To address this problem, LSTMs were developed (Hochreiter and Schmidhuber 1997).

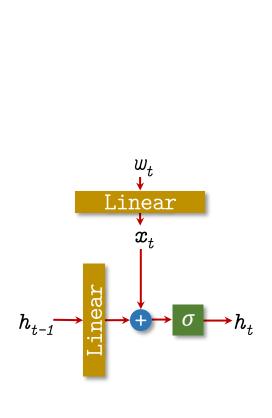


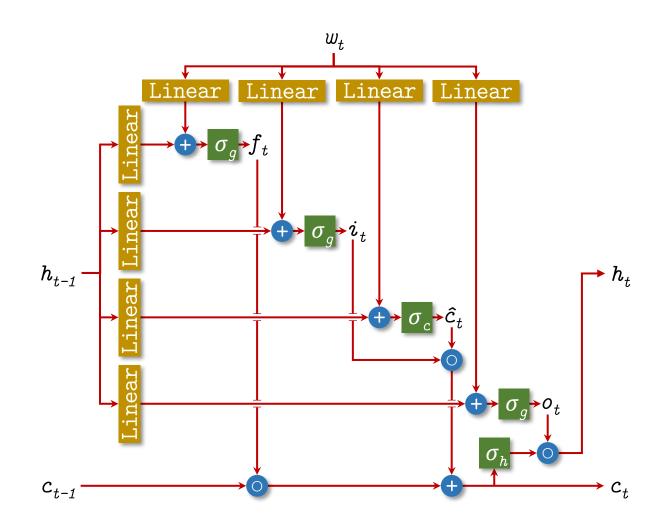
- ullet Key idea is that the updates to the c_i stream are additive.
- So gradients of c_i do not get very large or very small with increasing \emph{n} .
- How are c_i and h_i computed?



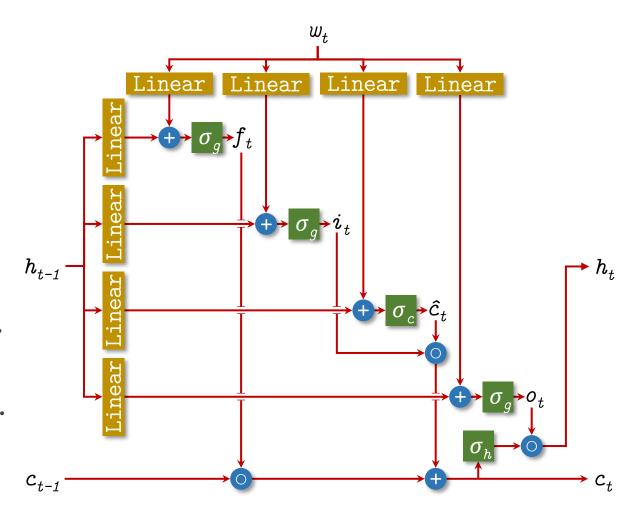
- Key idea is that the updates to the c_i stream are additive.
- So gradients of c_i do not get very large or very small with increasing n.
- How are c_i and h_i computed?







- Don't worry: You don't need to memorize this circuit diagram.
- It's easy enough to lookup.
- But the key idea is important:
- Updates to c_t are additive.
- Gradients with respect to c_t won't vanish or explode.



$$f_{t} = \sigma_{g}(W_{f}w_{t} + U_{f}h_{t-1} + b_{f})$$

$$i_{t} = \sigma_{g}(W_{i}w_{t} + U_{i}h_{t-1} + b_{i})$$

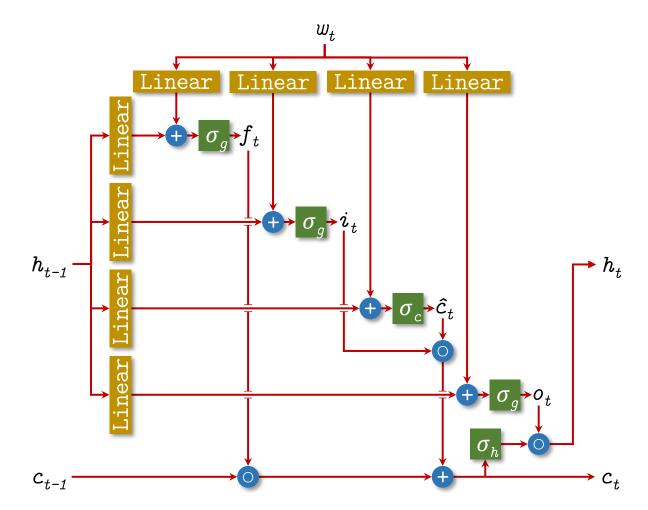
$$o_{t} = \sigma_{g}(W_{o}w_{t} + U_{o}h_{t-1} + b_{o})$$

$$\hat{c}_{t} = \sigma_{c}(W_{c}w_{t} + U_{c}h_{t-1} + b_{c})$$

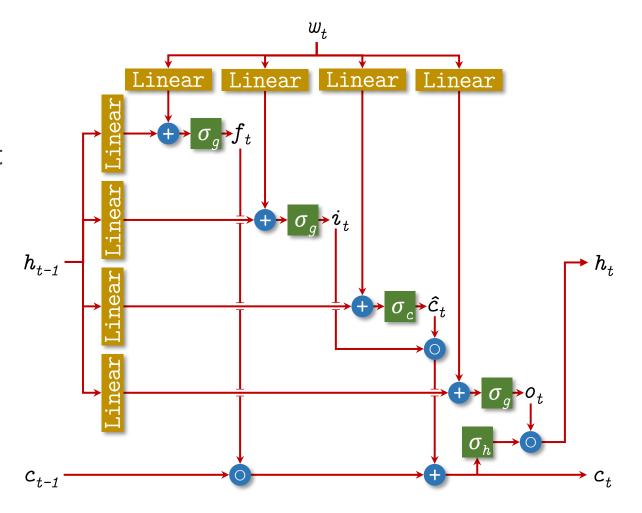
$$c_{t} = f_{t} \circ c_{t-1} + i_{t} \circ \hat{c}_{t}$$

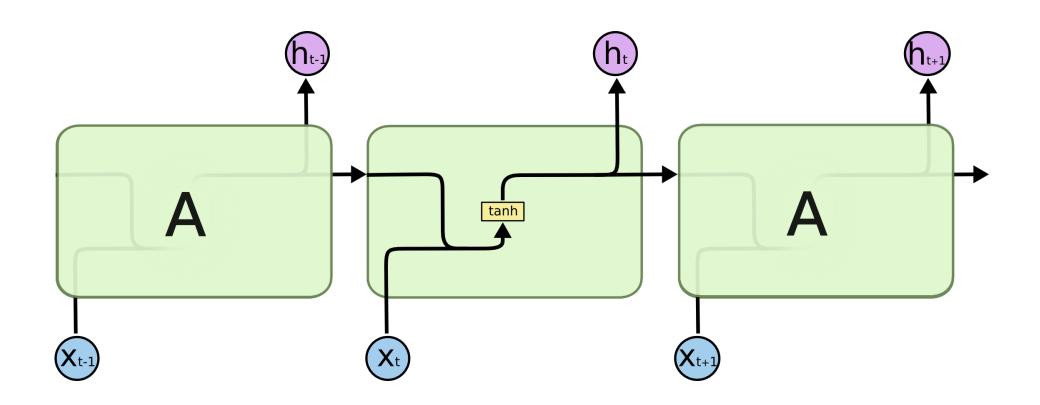
$$h_{t} = o_{t} \circ \sigma_{h}(c_{t})$$

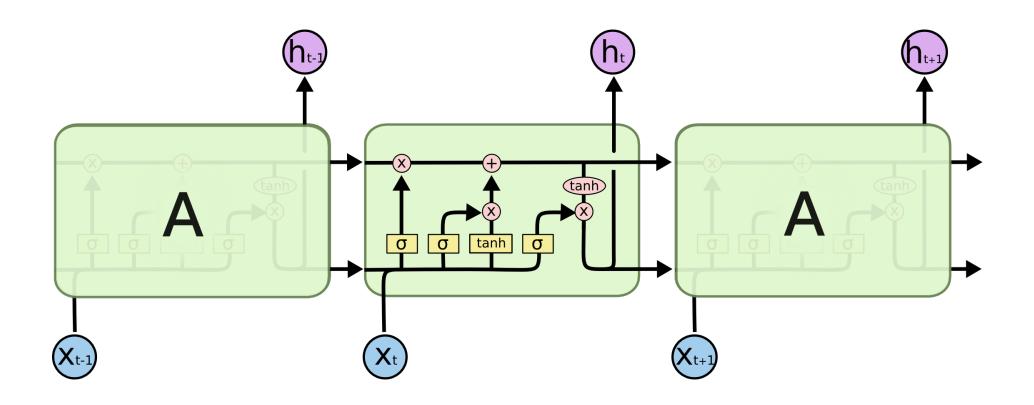
Traditionally, σ_g is a sigmoid, σ_c and σ_h are tanh.



- Subcircuits in the LSTM are referred to as "gates".
- For example, the subcircuit involving f_t is called the forget gate.
- The subcircuit involving \boldsymbol{i}_t is the input gate.
- The subcircuit involving o_t is the output gate.







- Train character-level LSTM on the language modeling task.
 - I.e., predict the next character given a sequence of previous characters.
 - Train on two datasets: War and Peace, and Linux kernel source code.
- We can inspect the activations in the cell state vector \boldsymbol{c}_t (i.e., activations of individual neurons).

- One neuron seems to predict the length of the current line.
- This is important when, e.g., you need to know when to predict n.
- Takeaway: LSTMs can model length.

```
Cell sensitive to position in line:

The sole importance of the crossing of the Berezina lies in the fact that it plainly and indubitably proved the fallacy of all the plans for cutting off the enemy's retreat and the soundness of the only possible line of action--the one Kutuzov and the general mass of the army demanded--namely, simply to follow the enemy up. The French crowd fled at a continually increasing speed and all its energy was directed to reaching its goal. It fled like a wounded animal and it was impossible to block its path. This was shown not so much by the arrangements it made for crossing as by what took place at the bridges. When the bridges broke down, unarmed soldiers, people from Moscow and women with children who were with the French transport, all--carried on by vis inertiae--pressed forward into boats and into the ice-covered water and did not, surrender.
```

- One neuron seems to keep track of when we're inside a quotation.
- This is important when, e.g., you need to know when to predict ", or when to predict sentences in first or second person.
- Seems to work even with very long quotations.

```
Cell that turns on inside quotes:

"You mean to imply that I have nothing to eat out of... On the contrary, I can supply you with everything even if you want to give dinner parties," warmly replied Chichagov, who tried by every word he spoke to prove his own rectitude and therefore imagined Kutuzov to be animated by the same desire.

Kutuzov, shrugging his shoulders, replied with his subtle penetrating smile: "I meant merely to say what I said."
```

- One neuron seems to keep track of when we're inside an if condition.
- This is useful to remember to close the if statement, and to predict comparisons rather than assignments.

```
Cell that robustly activates inside if statements:
static int __dequeue_signal(struct sigpending *pending, sigset_t *mask,
    siginfo_t *info)
{
    int sig = next_signal(pending, mask);
    if (sig) {
        if (current->notifier) {
            if (sigismember(current->notifier_mask, sig)) {
                clear_thread_flag(TIF_SIGPENDING);
                return 0;
        }
    }
    collect_signal(sig, pending, info);
}
return sig;
}
```

- One neuron seems to keep track of when we're inside a comment or a string.
- Useful to know to predict regular text rather than code.

- One neuron seems to keep track of the depth of the code.
- Useful to know how much to indent, or how many closing braces we need.

```
Cell that is sensitive to the depth of an expression:
#if def    CONFIG_AUDITSYSCALL
static inline int audit_match_class_bits(int class, u32 *mask)
{
    int    i;
    if (classes[class]) {
        for (i = 0; i < AUDIT_BITMASK_SIZE; i++)
          if (mask[i] & classes[class][i])
        return 0;
}
return 1;
}</pre>
```

- One neuron seems to predict the ends of some statements and expressions (but not all), and not the ends of comments.
- This neuron is more difficult to interpret.

```
Cell that might be helpful in predicting a new line. Note that it only turns on for some ")":
    char *audit_unpack_string(void **bufp, size_t *remain, si
    {
        char *str;
        if (!*bufp | | (len == 0) | | (len > *remain))
            return ERR_PTR(-EINVAL);
        /* of the currently implemented string fields, PATH_MAX
        * defines the longest valid length.
        */
        if (len > PATH_MAX)
        return ERR_PTR(-ENAMETOOLONG);
        str = kmalloc(len + 1, GFP_KERNEL);
        if (unlikely(!str))
        return ERR_PTR(-ENOMEM);
        memcpy(str, *bufp, len);
        str[len] = 0;
        *bufp += len;
        return str;
}
```

- But *most* neurons are not interpretable.
- There is no reason for models to be easily interpretable after training,
- Unless we specifically design the neural network otherwise.

```
/* Unpack a filter field's string representation from user-space
* buffer. */
char *audit_unpack_string(void **bufp, size_t *remain, size_t len)
{
   char *str;
   if (!*bufp || (len == 0) || (len > *remain))
    return ERR_PTR(-EINVAL);
   /* Of the currently implemented string fields, PATH_MAX
    * defines the longest valid length.
   */
```

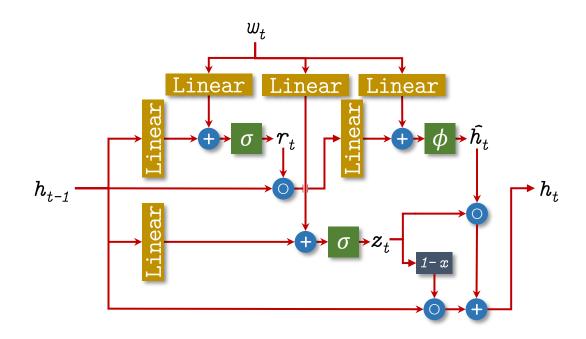
MECHANISTIC INTERPRETABILITY

- Mechanistic interpretability is the study of the internal computation of neural networks.
 - What algorithm has the network learned to solve the task?
 - "Reverse-engineering" the algorithm/mechanism learned by the network.
- Understanding neuron activations is akin to interpreting "intermediate variables" in the network's computation.
- But more work is needed to determine how these "intermediate variables" are related to each other.
 - How are they computed from the input/other intermediate variables?
 - How are they used to compute the output?

GATED RECURRENT UNITS

• A more recent variant of LSTMs is called the gated recurrent unit (GRU; Cho et al 2014).

- Simpler than the LSTM:
- Instead of having a separate "cell" state, perform linear updates to the hidden state.
- 2 gates (rather than 4).

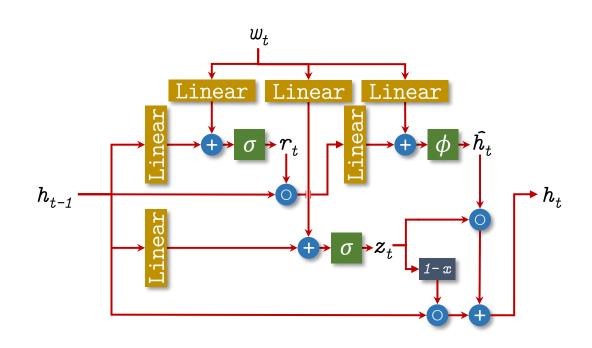


GATED RECURRENT UNITS

$$\begin{aligned} r_t &= \sigma(W_r w_t + U_r h_{t-1} + b_r) \\ z_t &= \sigma(W_z w_t + U_z h_{t-1} + b_z) \\ \hat{h}_t &= \phi(W_h w_t + U_h (r_t \circ h_{t-1}) + b_h) \\ h_t &= (1 - z_t) \circ h_{t-1} + z_t \circ \hat{h}_t \end{aligned}$$

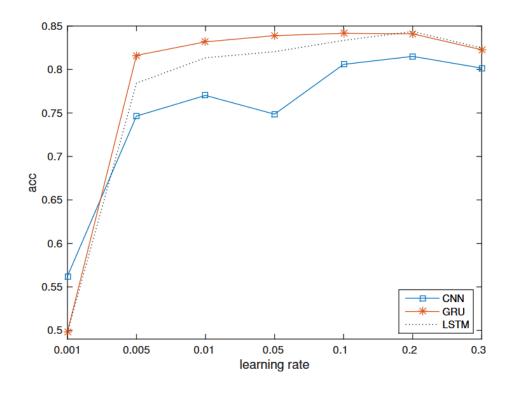
 σ is a sigmoid, and ϕ is tanh.

 z_t is between 0 and 1, so h_t is just a convex combination of the old state h_{t-1} , and the candidate state \hat{h}_t .

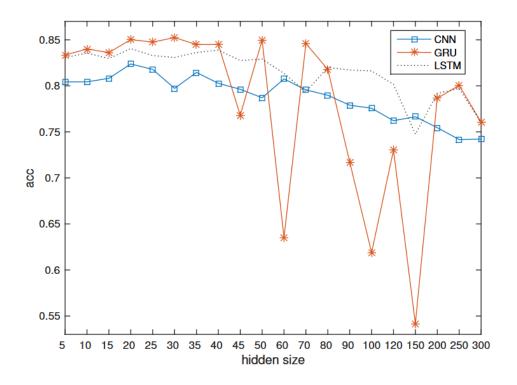


- Which one is better?
- There is no one clear winner.
- It depends on the task, data, hyperparameters, etc.
- Let's take a look at some examples.
- Yin et al. 2017 trained three models on two tasks:
 - Models: LSTM, GRU, and CNN (convolutional neural network)
 - Tasks: Sentiment analysis, multiple-choice question answering

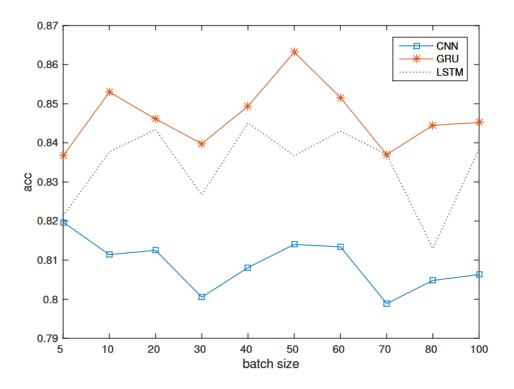
• Accuracy vs learning rate in sentiment analysis task.



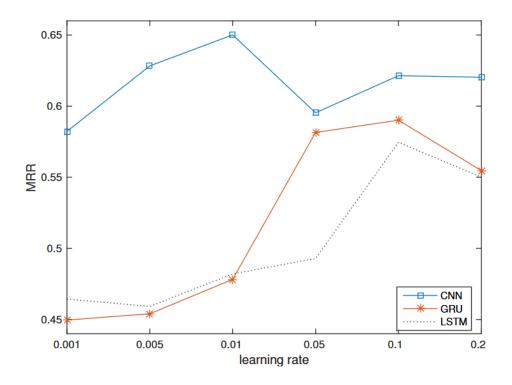
• Accuracy vs hidden state dimension in sentiment analysis task.



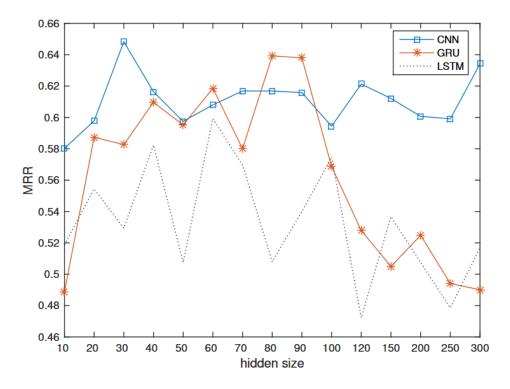
• Accuracy vs batch size in sentiment analysis task.



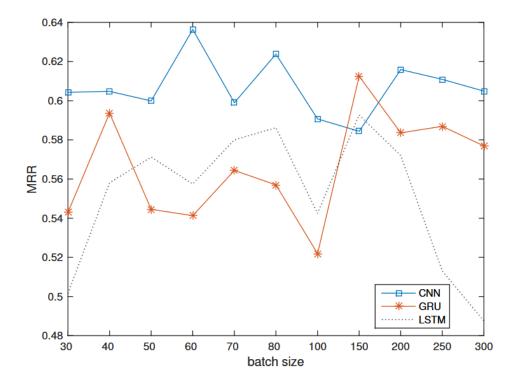
• Mean reciprocal rank vs learning rate in multiple-choice QA task.



• Mean reciprocal rank vs hidden state dimension in multiple-choice QA task.



• Mean reciprocal rank vs batch size in multiple-choice QA task.



RNN SUMMARY

- GRUs can achieve comparable performance to LSTMs despite being simpler.
- Some terminology clarification:
 - GRUs are often considered a special case of LSTMs.
 - Both GRUs and LSTMs are often considered special cases of RNNs.
 - So "RNN" can be used as an umbrella term to include any method that processes sequential information one element at a time.
 - I.e., word-by-word, character-by-character

RNN DISADVANTAGES

- What are some disadvantages of RNNs (including LSTMs, GRUs)?
- They are not easily parallelizable.
 - If I want to compute the n-th hidden state, I need to process n tokens sequentially.
 - This is made even worse with deep RNNs.
 - The hidden state of the next layer is dependent on the hidden state of the previous layer.
- This limits their ability to scale to very large datasets. (but can still be done)
- Next lecture, we will look at transformers, which do not have this limitation.

