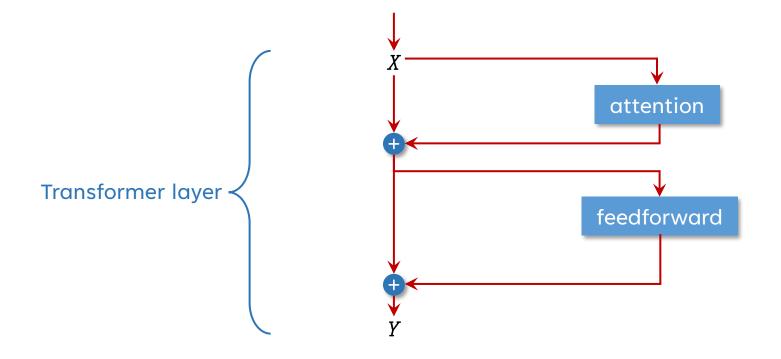


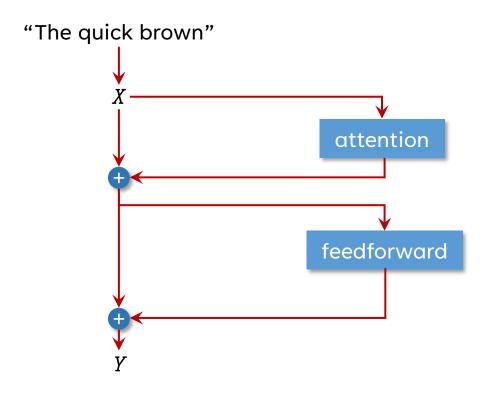
Lecture 7: Transformers II

PREVIOUS LECTURE: TRANSFORMERS



- Suppose we are training a transformer on a classification task, so we have a softmax operation at the end of the network.
- Also suppose the input embeddings have large magnitude,
- It's very likely that the magnitude of the embeddings stays large throughout the transformer layers, up to the last softmax operation.
- Recall that the derivative of the softmax is close to zero if the input is a large positive or negative value.
 - Hint: The logistic function (i.e., sigmoid) is equivalent to softmax in two dimensions.
- Thus, in this example, the gradient would be very close to zero, and training would be extremely slow.

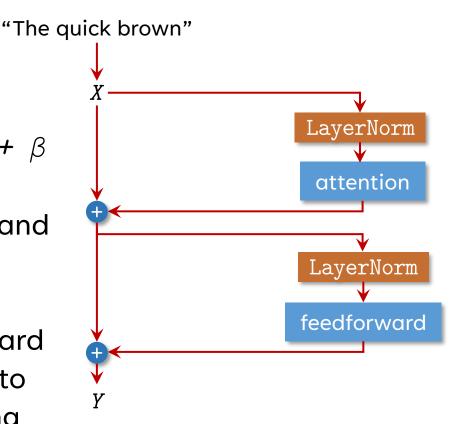
- Thus, transformers with many layers can also sometimes suffer from vanishing gradients.
- To avoid this, transformers use layer normalization.



 $\text{LayerNorm}(x_i) = \frac{x_i - avg(x_i)}{\sqrt{var(x_i) + \varepsilon}} \circ_{\gamma} + \beta$

Where ε is a small fixed constant, γ and β are vectors of learnable weights.

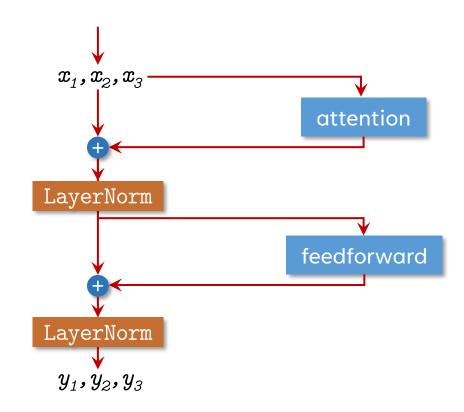
Since we scale the input by its standard deviation, layer normalization helps to prevent the activations from attaining very large positive or negative values.



POST-LAYER NORMALIZATION

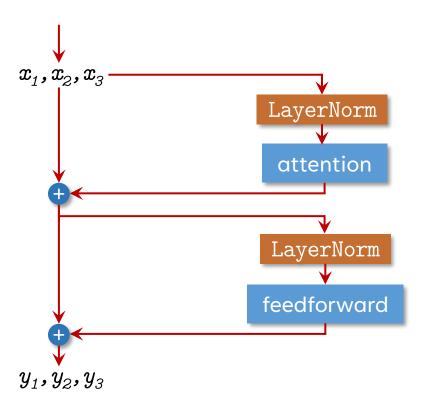
The original transformer paper used post-layer normalization.

Layer normalization was applied on the residual stream (i.e., *after* residual connection).

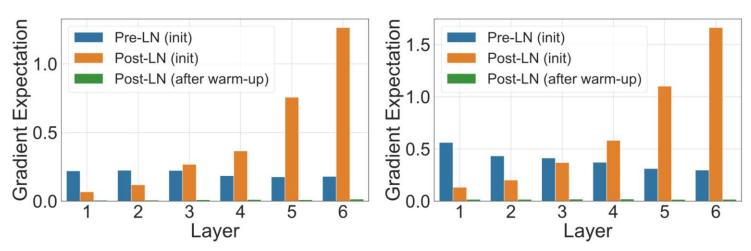


[Vaswani et al., 2017]

Xiong et al., 2020, proposed moving the layer normalization *before* the attention and FF blocks.

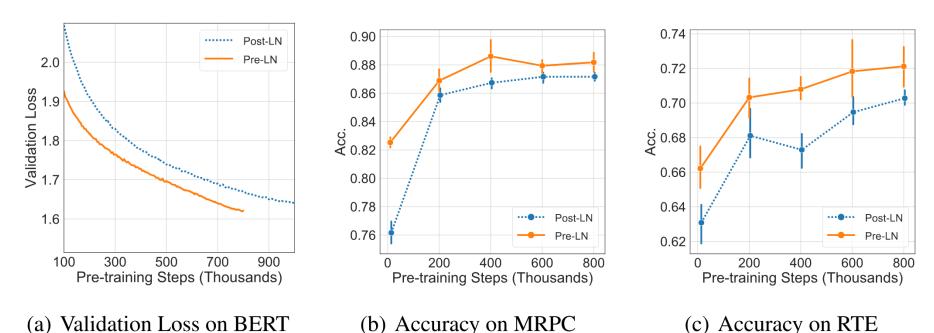


- Xiong et al., 2020, showed that the magnitudes of the gradients are more uniform across layers when using pre-layer normalization.
- Hypothesis: Learning occurs at a more uniform rate across layers when using pre-layer norm.

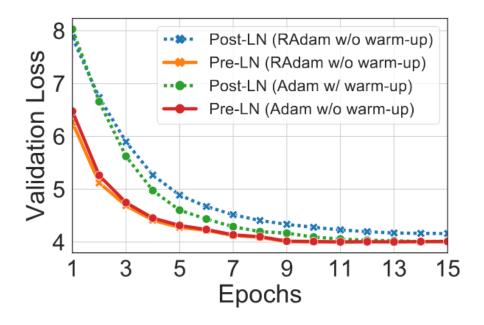


(a) W^1 in the FFN sub-layers (b) W^2 in the FFN sub-layers

• Measure empirical performance on masked language modeling, semantic similarity (Microsoft Research Paragraph Corpus), and textual entailment (Recognizing Textual Entailment dataset).

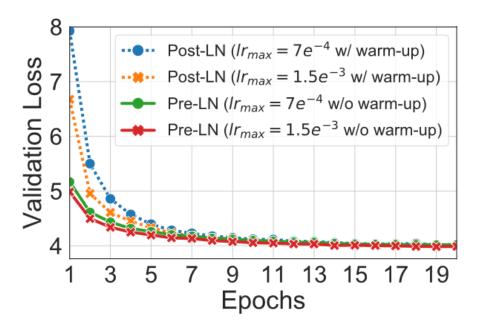


• Measure empirical performance on machine translation.



(a) Validation Loss (IWSLT)

• Measure empirical performance on machine translation.



(c) Validation Loss (WMT)

RMS NORMALIZATION

• Zhang and Sennrich, 2019, proposed a simpler alternative to layer normalization, called root mean square layer normalization, or RMSNorm.

$$\text{LayerNorm}(x_i) = \frac{x_i - avg(x_i)}{\sqrt{var(x_i) + \varepsilon}} \circ_{\gamma} + \beta$$

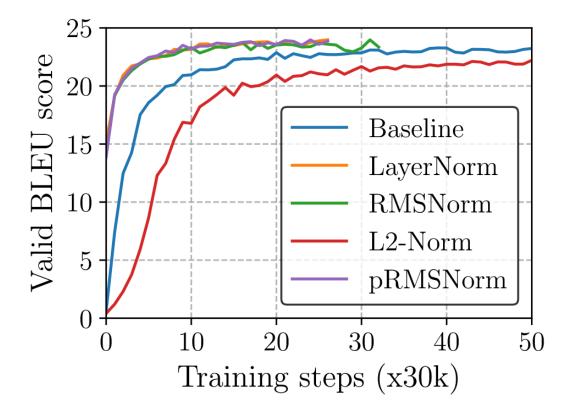
where ε is a small fixed constant, γ and β are vectors of learnable weights.

$$\text{RMSNorm}(x_i) = \frac{x_i}{\text{RMS}(x_i)} \circ_Y \text{ where } \text{RMS}(x_i) = \sqrt{\frac{1}{n} \sum_{j=1}^n x_{i,j}^2}$$

Note that RMSNorm is faster to compute.

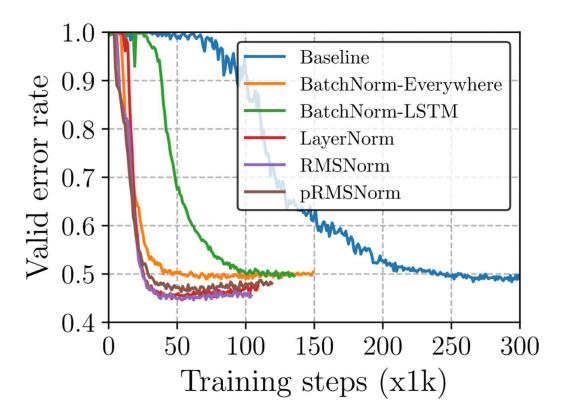
RMS NORMALIZATION

• Measure empirical performance on machine translation.



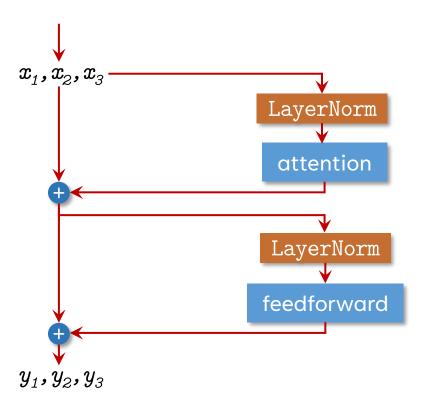
RMS NORMALIZATION

• Measure empirical performance on question answering.



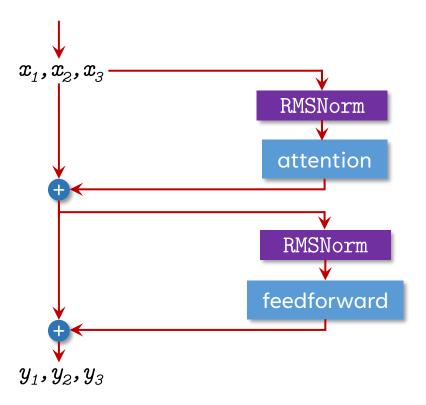
PRE-LAYER NORMALIZATION AND RMSNORM

• GPT-2 used pre-layer normalization.

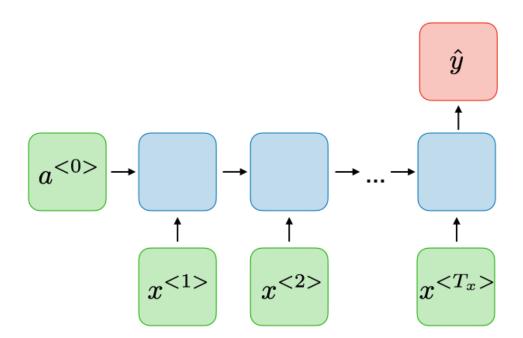


PRE-LAYER NORMALIZATION AND RMSNORM

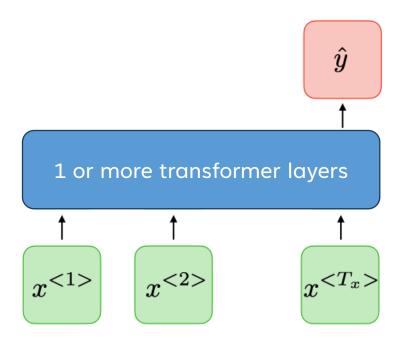
- GPT-2 used pre-layer normalization.
- Recent models (e.g., LLaMA and DeepSeek) typically use pre-layer normalization with RMSNorm.



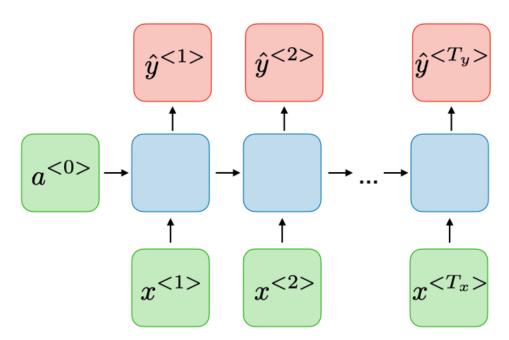
• Recall that RNNs can be used in a wide variety of architectures.



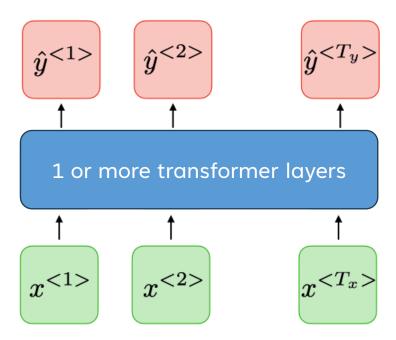
- Recall that RNNs can be used in a wide variety of architectures.
- Transformers can similarly be a component in lots of different models.



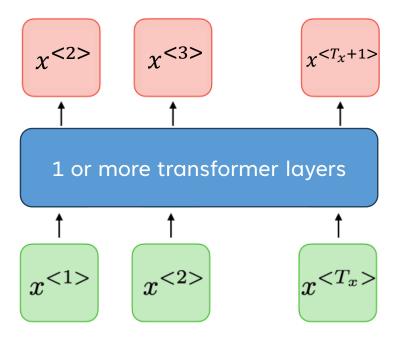
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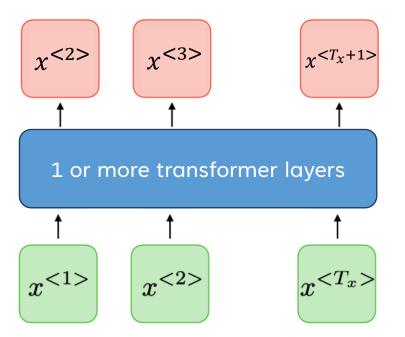
In the language modeling task, we often predict n tokens, where the i^{th} output token corresponds to the $i+1^{th}$ input token.

The loss is computed as the sum of the losses of all output tokens.

Often called autoregressive or causal language modeling.

WHY THE CAUSAL MASK?

- Recall that RNNs can be used in a wide variety of architectures.
- Transformers can similarly be a component in lots of different models.



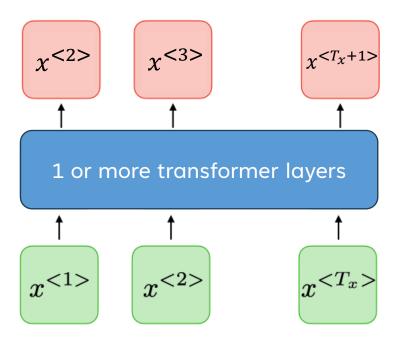
This motivates the causal mask.

We want $x^{< i>}$ to only attend to tokens that come before it.

Otherwise, it can simply cheat by copying $x^{(i+1)}$.

WHY THE CAUSAL MASK?

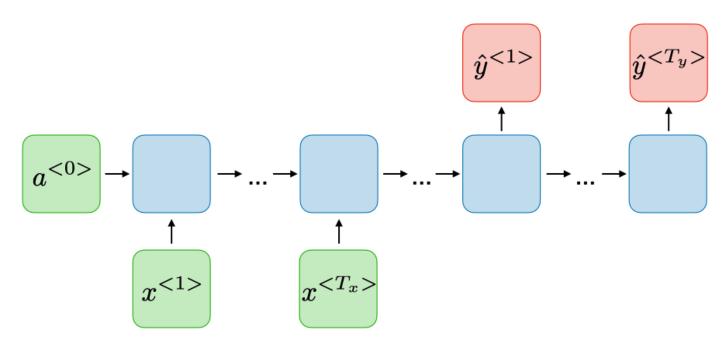
- Recall that RNNs can be used in a wide variety of architectures.
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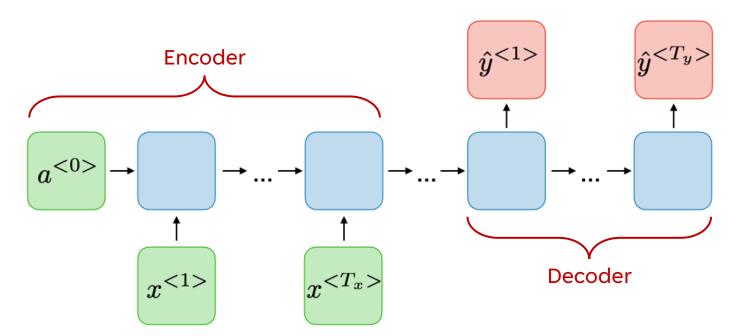
With or without the causal mask, the model still must predict the token after the last token.

The model can't "cheat" here by attending to future tokens.

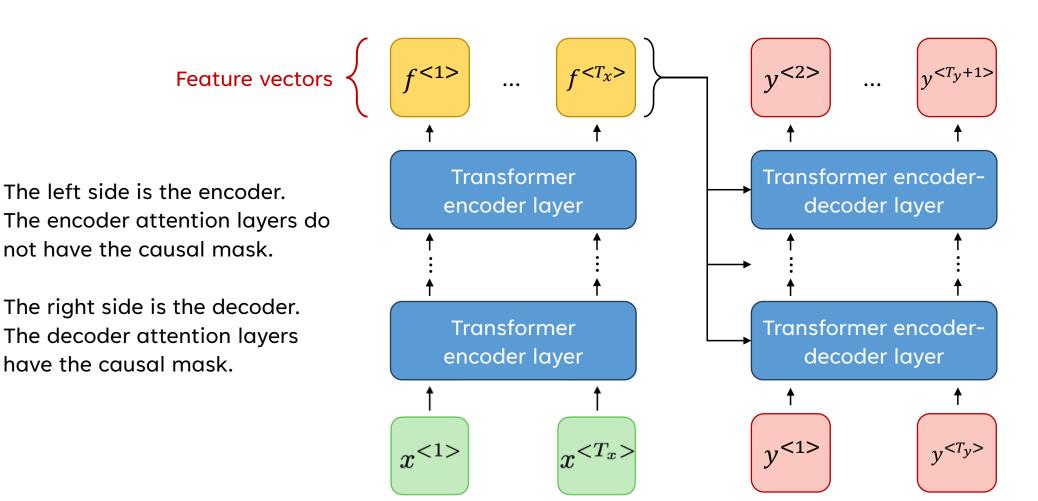
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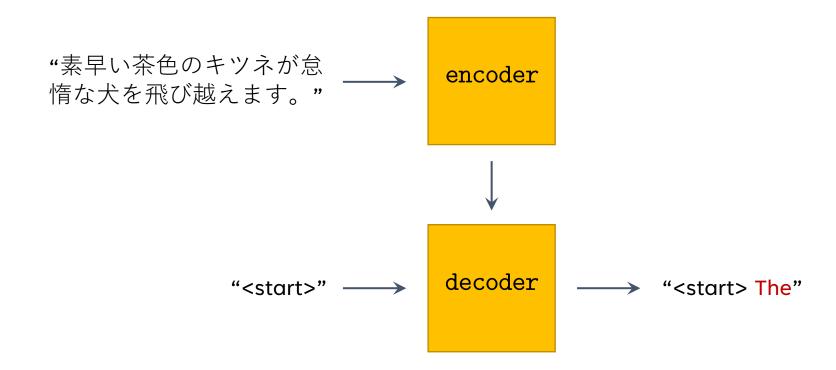


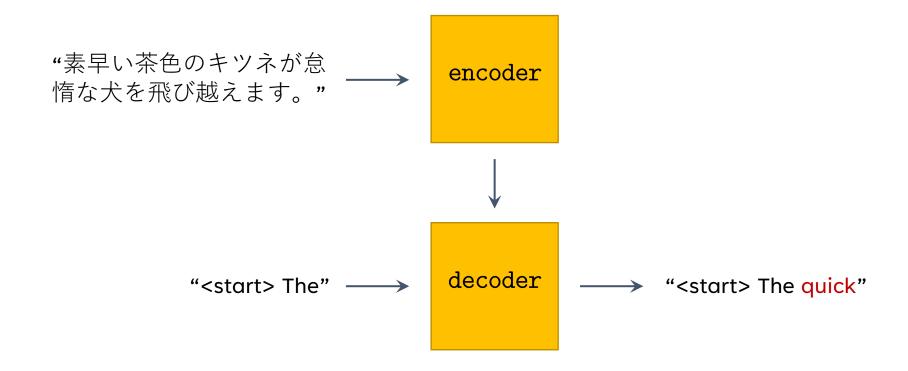
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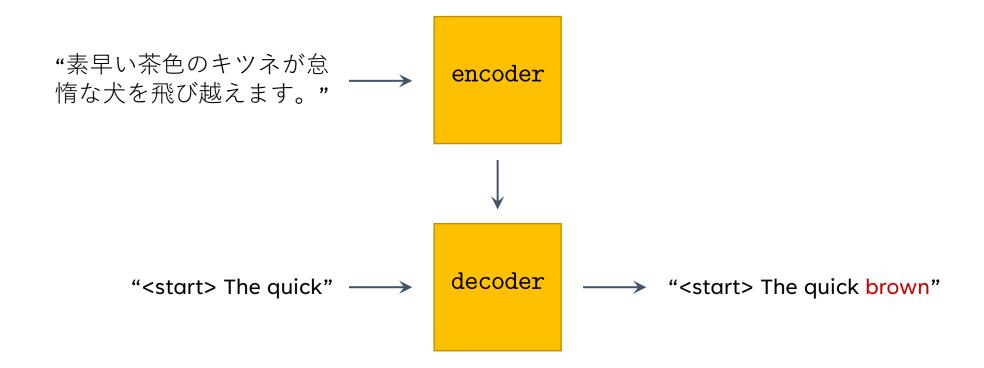


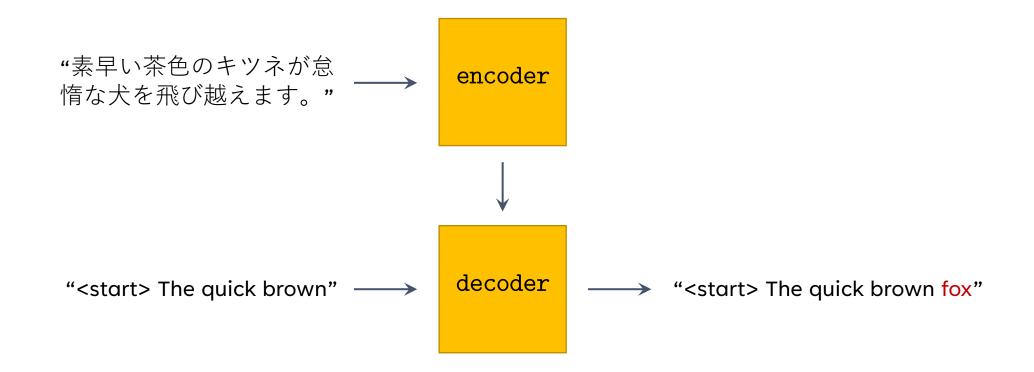
TRANSFORMER ENCODER-DECODER

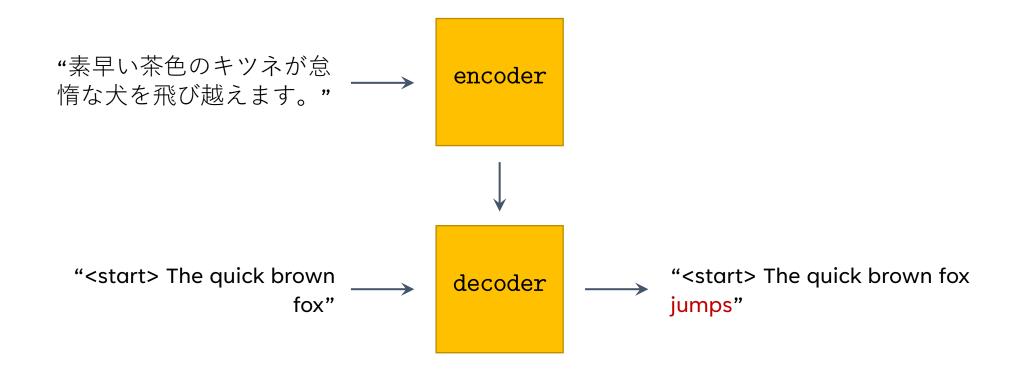


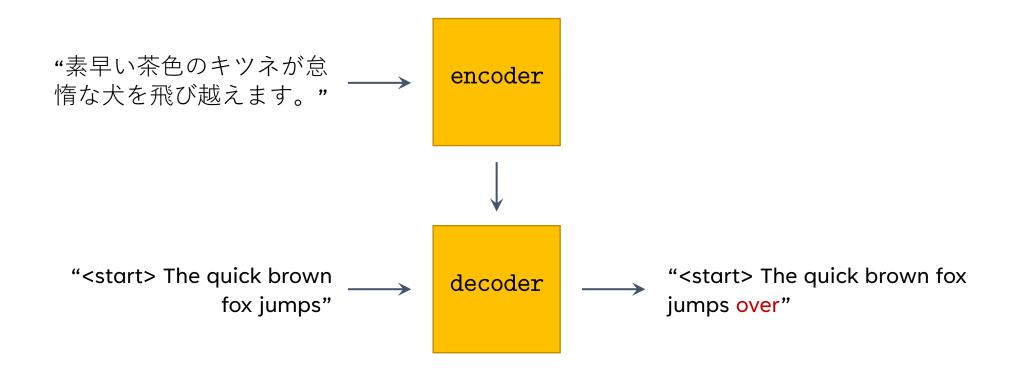


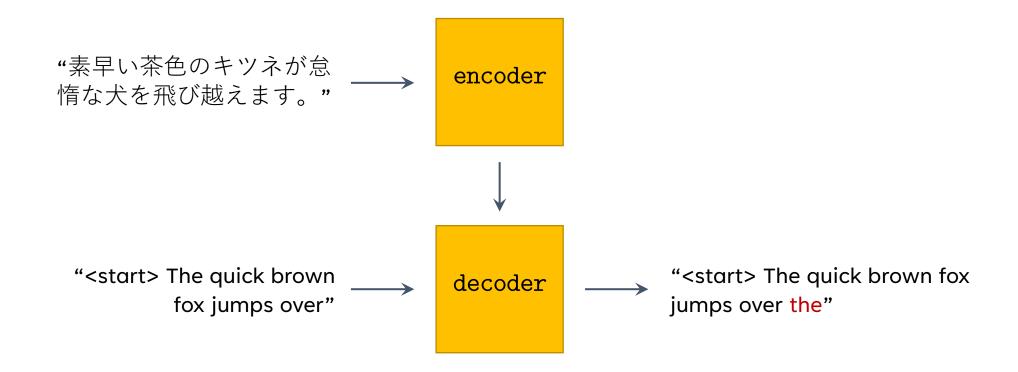


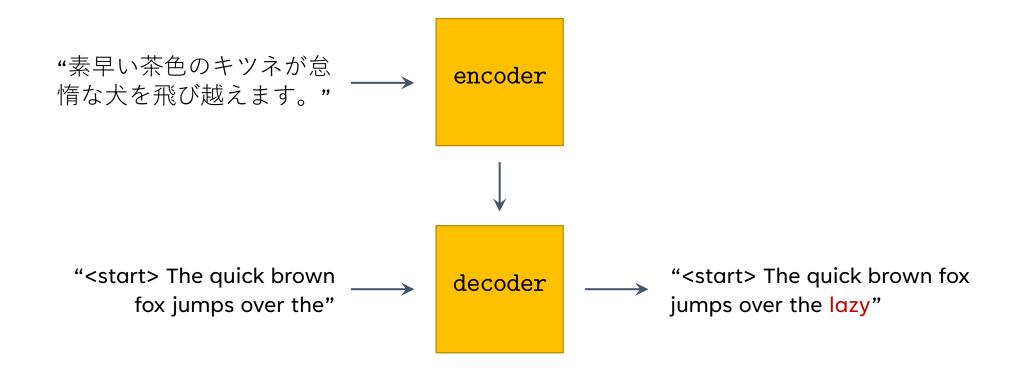


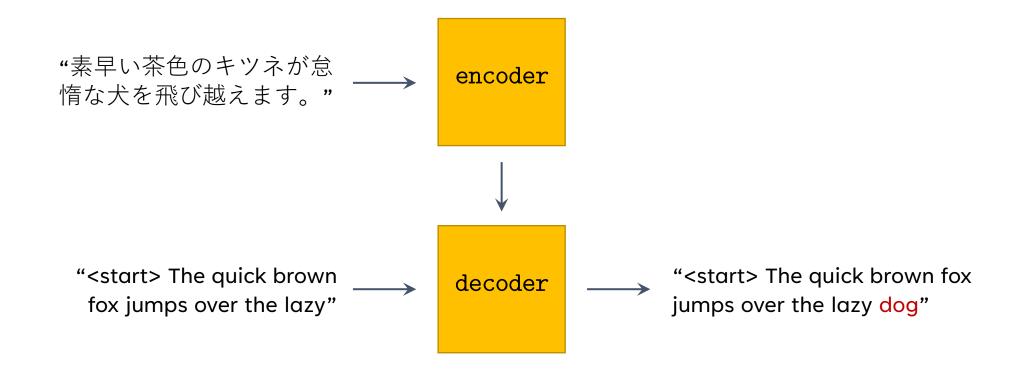




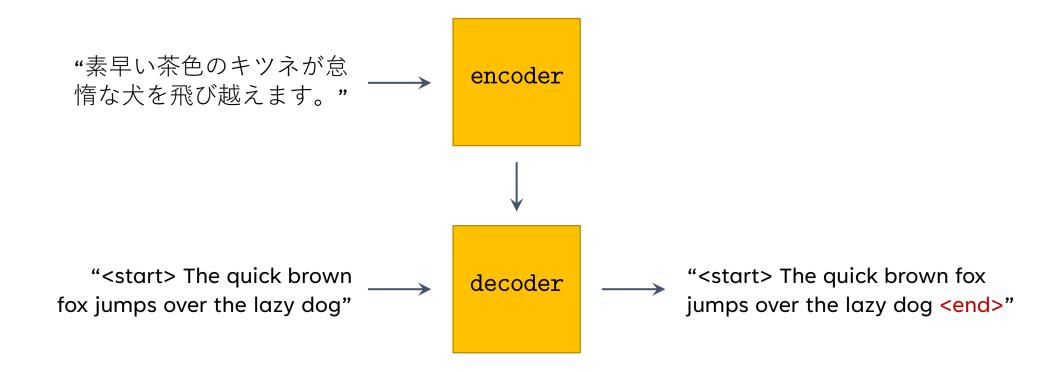






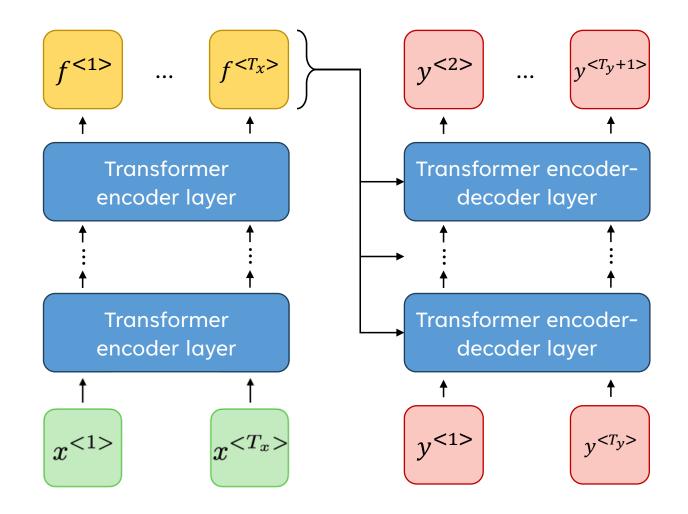


ENCODER-DECODER

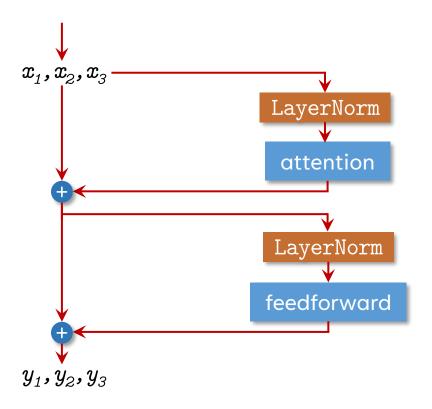


TRANSFORMER ENCODER-DECODER

How does the transformer encoder-decoder layer incorporate information from the encoder (i.e., features)?



TRANSFORMER LAYER

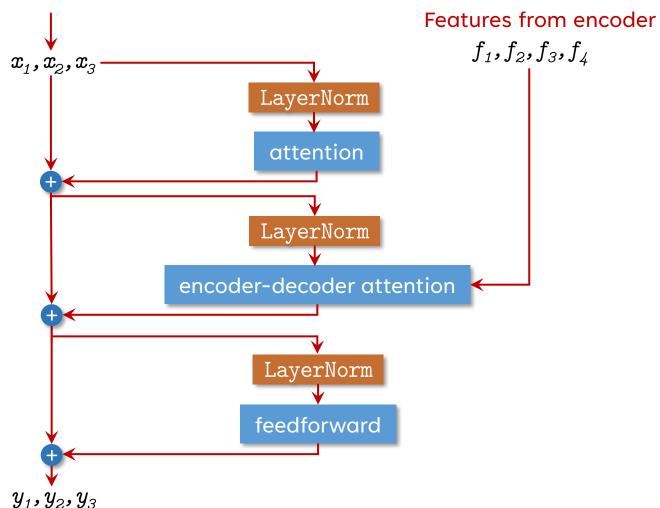


TRANSFORMER ENCODER-DECODER LAYER

The first attention layer has a causal mask.

The encoder-decoder attention layer does not.

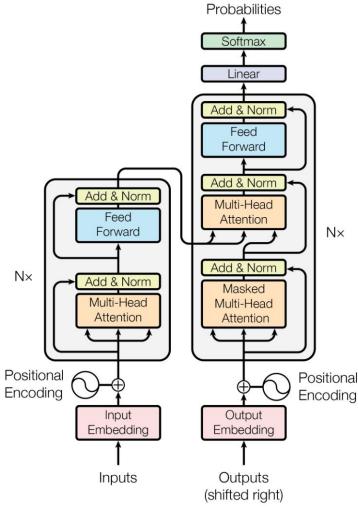
What does the encoder-decoder attention layer look like?



TRANSFORMER ENCODER-DECODER LAYER

Output

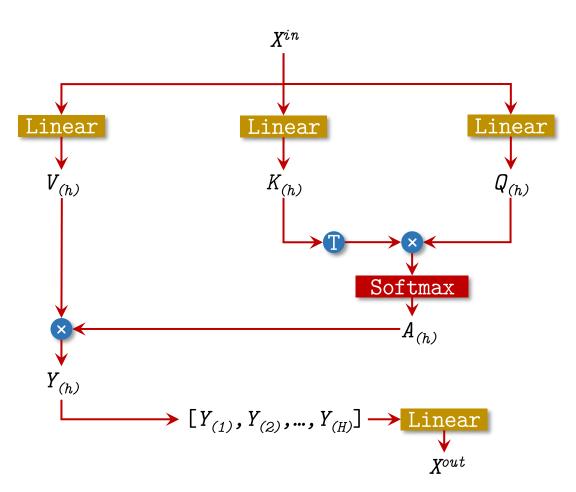
This is Figure 1 from the original transformer paper.



[Vaswani et al., 2017] 41

ATTENTION LAYER

Recall this is the circuit diagram for the multi-head attention component.

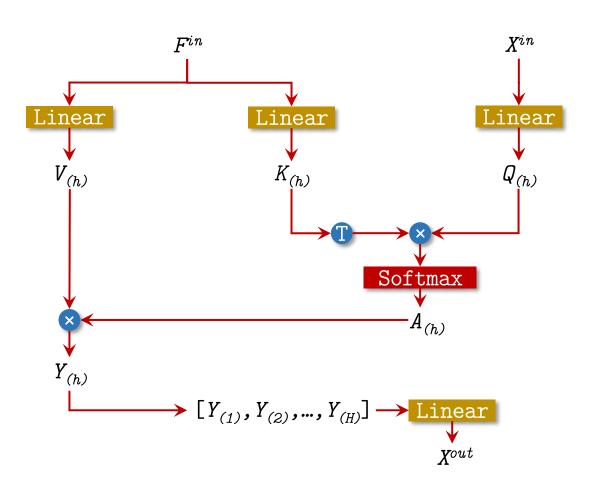


ENCODER-DECODER ATTENTION LAYER

 X^{in} are the inputs from the previous decoder layer.

 F^{in} are the inputs from the encoder (i.e., features).

 X^{in} is $n imes d_{model}$. F^{in} is $m imes d_{model}$. $V_{(h)}$ is $m imes d_{attn}$. $K_{(h)}$ is $m imes d_{attn}$. $Q_{(h)}$ is $n imes d_{attn}$. $A_{(h)}$ is n imes m. $Y_{(h)}$ is $n imes d_{attn}$. X^{out} is $n imes d_{model}$.

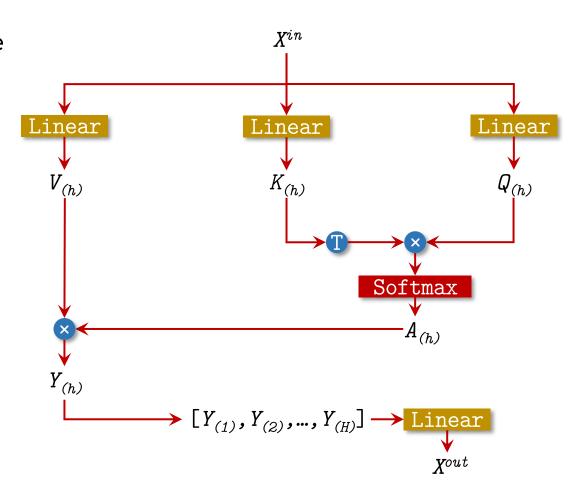


ENCODER-ONLY AND DECODER-ONLY ATTENTION LAYER

So the attention layer where there is only 1 input is referred to as encoder-only or decoder-only.

Encoder-only attention layers do not have a causal mask.

Decoder-only attention layers have a causal mask.

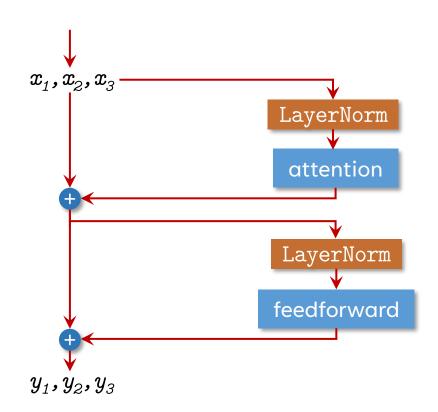


ENCODER-ONLY AND DECODER-ONLY TRANSFORMER LAYER

Similarly, a transformer layer without encoder-decoder attention is called an encoder-only or decoder-only transformer layer,

depending on whether it has a causal mask.

Encoder-only transformers are also called bidirectional transformers.



EXAMPLE ENCODER-DECODER TRANSFORMER MODELS

- Some example encoder-decoder models: (trivia)
 - BART (Lewis et al., 2019)
 - Up to 400M parameters.
 - T5 (Raffel et al., 2020)
 - Up to 11B parameters.
 - UnifiedQA (Khashabi et al., 2020)

EXAMPLE ENCODER-ONLY TRANSFORMER MODELS

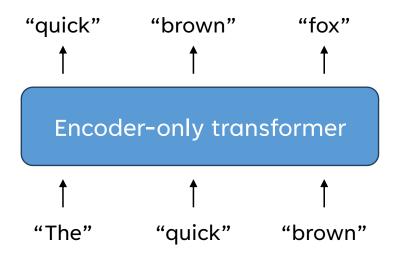
- Some example encoder-only models: (trivia)
 - BERT (Devlin et al., 2018)
 - Up to 355M parameters.
 - RoBERTa (Liu et al., 2019)
 - Up to 355M parameters.
 - DeBERTa (He et al., 2021)
 - Up to 1.5B parameters.

EXAMPLE DECODER-ONLY TRANSFORMER MODELS

- Modern language models are decoder-only models. (trivia)
 - GPT-2 (Radford et al., 2019)
 - Up to 1.5B parameters.
 - GPT-3 (Brown et al., 2020)
 - Up to 175B parameters.
 - GPT-4 (OpenAI, 2023)
 - (unofficial) Up to 1.7T parameters (111B per expert).
 - LLaMA 3 (Meta, 2024)
 - Up to 405B parameters.
 - DeepSeek-V3 (DeepSeek-AI, 2024)
 - Up to 671B parameters (37B per expert).

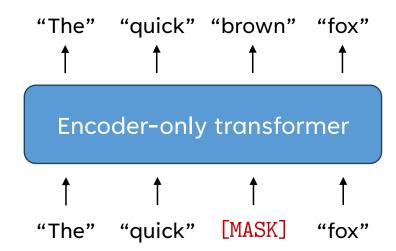
TRAINING ENCODER-ONLY MODELS

- How are encoder-only models like BERT trained?
- We can't use autoregressive language modeling since without the causal mask, encoder-only transformers can "cheat" by copying the next token.



TRAINING ENCODER-ONLY MODELS

- How are encoder-only models like BERT trained?
- Instead, we use the masked language modeling task.
- Randomly replace some percentage of the input words with [MASK].
- The model's task is to fill in the masked words/tokens.



TRAINING ENCODER-ONLY MODELS

- How are encoder-only models like BERT trained?
- Measure the loss function only on the masked tokens.

